

Course name : <b>Probabilistic System Analysis</b>		
Type of study: <b>Mathematics</b>	Type of study: <b>Full-time</b>	Examination: <b>Assignment</b>
Course characteristics: <b>Compulsory</b>	Level: <b>First (B.Sc.)</b>	Year: <b>Spring Semester</b>
Type of classes: <b>lectures, laboratory, tutorials</b>	Hours per week: <b>2 L, 2 Lab, 1T</b>	ECTS points: <b>6 ECTS</b>

## COURSE DESCRIPTION

### COURSE OBJECTIVE

- C1.** Making the students familiar with the elements of the theory and methods of probability useful in engineering problems.
- C2.** Making the students familiar with the elements of the statistical methods.
- C3.** Introducing the students into using the computer methods in probability and statistics.

### PREREQUISITES/ ASSUMED BACKGROUND

1. Course of the calculus of one variable

### LEARNING OUTCOMES and COMPETENCES TO BE ATTAINED

- LO1.** – student is familiar with the basics of probability; student understands the need of probability in statistics.
- LO2.**– student is familiar with the introductory methods of a point and interval estimation; student is able to use Maple in solving simple estimation problems.
- LO3.**– student is familiar with the introductory methods of a hypothesis testing; student is able to use Maple in solving problems of this type.

### COURSE CONTENT

<b>Lecture - Topics</b>	<b>Hours</b>
<b>L 1</b> – Course introduction. The subject of statistics, the need of probability. Types of data	<b>2</b>
<b>L 2</b> – Methods for describing data	<b>2</b>
<b>L 3</b> – The numerical descriptive measures	<b>2</b>
<b>L 4</b> – The numerical descriptive measures, cont. , random experiment, events, sample spaces	<b>2</b>
<b>L 5</b> – Probability – axioms and properties	<b>2</b>
<b>L 6</b> – Conditional probability, total probability Bayes' theorem	<b>2</b>
<b>L 7</b> – Independence. Introduction to the random variables. Discrete random variables.	<b>2</b>
<b>L 8</b> – Probability distribution for discrete random variable, expected value. Basic discrete distributions.	<b>2</b>
<b>L 9</b> – Continuous random variables. Probability distribution for continuous random variables, expected value. Basic continuous distributions.	<b>2</b>
<b>L 10</b> – Basic continuous distributions cont. Introduction to sampling distributions.	<b>2</b>

<b>L 11</b> – Introduction to sampling distributions cont. The law of large numbers. The central limit theorem.	<b>2</b>
<b>L 12</b> – The point estimation	<b>2</b>
<b>L 13</b> – The confidence intervals	<b>2</b>
<b>L 14</b> – Test of hypothesis: single sample	<b>2</b>
<b>L 15</b> – Test of hypothesis: two samples	<b>2</b>
<b>Σ</b>	<b>30</b>
<b>Tutorials – Topics</b>	<b>Hours</b>
<b>T 1</b> –Types of data	<b>1</b>
<b>T 2</b> – Graphical description of data	<b>1</b>
<b>T 3</b> – The mode, the arithmetic mean	<b>1</b>
<b>T 4</b> – The range of data. Variance and standard deviation	<b>1</b>
<b>T 5</b> – Variance and standard deviation cont., Interpretation of the standard deviation.	<b>1</b>
<b>T 6</b> – Property of probability, Bayes’ rule	<b>1</b>
<b>T 7</b> – Independence	<b>1</b>
<b>T 8</b> – Discrete random variables: calculating the expected value and the standard deviation	<b>1</b>
<b>T 9</b> – Discrete random variables: applications to the real world problems	<b>1</b>
<b>T 10</b> – Continuous random variables: calculating the expected value and the standard deviation	<b>1</b>
<b>T 11</b> – Continuous random variables: applications to the real world problems	<b>1</b>
<b>T 12</b> – Point estimation, maximum likelihood method	<b>1</b>
<b>T 13</b> – A confidence interval for a population mean – a large sample case	<b>1</b>
<b>T 14</b> – Test of hypothesis about a population mean – a large sample case	<b>1</b>
<b>T 15</b> – The power of a test, p-value of a test	<b>1</b>
<b>Σ</b>	<b>15</b>
<b>Laboratory - Topics</b>	<b>Hours</b>
<b>Lab 1</b> – Review of integration	<b>2</b>
<b>Lab 2</b> – Methods for describing data	<b>2</b>
<b>Lab 3</b> – Calculating numerical descriptive measures	<b>2</b>
<b>Lab 4</b> –Basic combinatorics	<b>2</b>
<b>Lab 5</b> – Classical definition of probability	<b>2</b>
<b>Lab 6</b> – Conditional probability, total probability, Bayes’ theorem, independence	<b>2</b>
<b>Lab 7</b> –Discrete random variables.	<b>2</b>
<b>Lab 8</b> – Probability distribution for discrete random variable, expected value.	<b>2</b>
<b>Lab 9</b> – Continuous random variables. Probability distribution for continuous random variables, expected value.	<b>2</b>
<b>Lab 10</b> – Generating pseudorandom numbers	<b>2</b>
<b>Lab 11</b> – Various problems concerning discrete and continuous random variables	<b>2</b>
<b>Lab 12</b> – The point estimation	<b>2</b>
<b>Lab 13</b> – The confidence intervals	<b>2</b>
<b>Lab 14</b> – Test of hypothesis: single sample	<b>2</b>
<b>Lab 15</b> – Test of hypothesis: two samples	<b>2</b>
<b>Σ</b>	<b>30</b>

#### TEACHING TOOLS

1. – lecture

2. – tutorials
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3. – computer laboratory
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### RECOMMENDED AND ADDITIONAL BIBLIOGRAPHY

Lecture notes
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Ramachandran, K. M., Tsokos.C.P., <i>Mathematical statistics with applications</i> , Elsevier Academic Press, 2009
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J.T.McLeve, P.G.Benson, <i>Statistics for business and economics</i> , Macmillan, London 1988 and later issues
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### TEACHERS

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### ADDITIONAL NOTES

Links to course unit teaching materials can be found on the <http://www.pcz.pl/english/ects-subjects> website for current students.